

## *University mathematics education*

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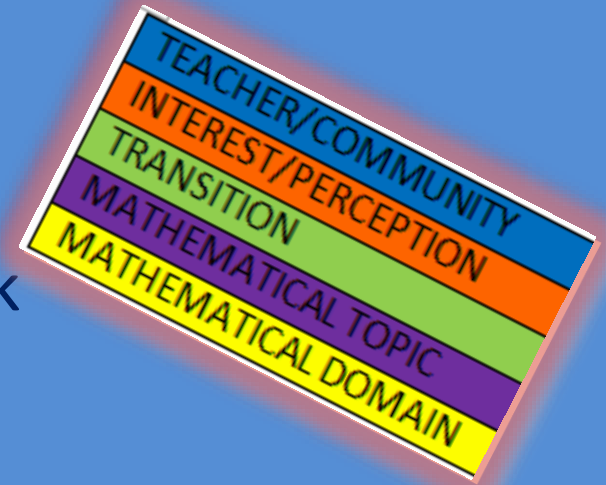
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# Welcome!

- 17:00 Welcome: from CERME7 to CERME8, and beyond!
- 17:10 Introduction to WG14 Subgroups  
(CW, EN, IB, AGM, GG)  
Schedule for Sessions 1-7
- 17:20 Introduction to today's group-work  
Splitting in small groups
- 17:30 Group-work
- 18:15 Small group presentations by nominated participant
- 18:45 Preliminary discussion of post-CERME8 collaboration
- 19:00 Closing



# WG14: University mathematics education Session Outline



	February 5th Tuesday	February 6th Wednesday	February 7th Thursday	February 8th Friday	February 9th Saturday	February 10th Sunday
8 30	YERME DAY	YERME DAY  ERME meets Young Researchers Reception  Opening Ceremony  Plenary Talk Paolo Boero Coffee break WG Session 1  <b>All</b>  Dinner	WG Session 2  <b>Carl</b>	WG Session 4  <b>Irene</b>	WG Session 6  <b>Ghislaine</b>	WGs Report 1
9 00			WGs Report 2			
9 30			WGs Report 2			
10 00			Coffee break			
10 30			Joint Report ERME – EMS EC			
11 00			Coffee Break			
11 30			Plenary Talk Alain Kuzniak	WG Session 5  <b>Alejandro</b>	Plenary Talk Candia Morgan	Closing Ceremony
12 00			Lunch (ERME will welcome newcomers from 13.15 till 14.00.)	Lunch	Lunch	Lunch + Departures
12 30			Poster session	Excursion departure	ERME General Assembly	
13 00			Coffee Break		Coffee break	
13 30			WG session 3  <b>Elena</b>	WG Session 7  <b>All</b>		
14 00			Forum	Excursion return	Results of elections	
14 30			Dinner	Dinner	Free time	
15 00			Gala Dinner			
15 30						
16 00						
16 30						
17 00						
17 30						
18 00						
18 30						
19 00						
19 30						
20 00						
20 30						
21 00	Live Music	Turkish Contributions to Mathematical Sciences Cem Tezer	Live Music			

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**\* Work in four groups each led by GG, AGM, IB and EN.** Subgroup CW includes 5 papers, 3 by co-leaders IB, GG and EN. These papers will be discussed within these co-leaders' small groups. The authors of the other two CW papers (Jaworski, Pinto) will discuss their paper within the subgroup they choose to attend. CW will join the IB group in which his paper belongs. Participants who are not authors can choose their groups freely.

**\*\*Small group-work agenda**

*Individual introductions*

Please include your interests and expectations from the WG.

*Preliminary discussion of papers*

Please focus on the subgroup papers and any extra papers as in \*.

Focus on initial observations of commonalities and differences; and, on making the most of the time dedicated to these papers in Sessions 2-6.

Welcome by co-leader

*Paper Reminder-Presentations\** and *Reactions\**

Discussion of papers in small groups\*\*

Plenary summaries of small-group discussions

Plenary discussion

Closing

*\*Maximum 5 minutes long assisted (optional) by one slide of at least 20pt font size.*

**\*\***20 minutes

## **Part I: Preparing Sunday's WG14 presentation**

- Observations from co-leaders on themes across Sessions 2-6
- Discussion: the structure of Sunday's WG presentation
- Group-work on presentation sections
- Plenary discussion of group-work outputs and presentation drafting

## **Part II: Post-conference collaboration**

- Preparations for the Proceedings
- *Beyond CERME8: Special Issue Proposal, PME37 etc.*

8.30-9.20 Paper reminder presentations + reactions (5'+5')

Biza - Pinto - Gueudet - Jaworski - Nardi

9.25-10.00 Discussion of five papers each in one group

NB: each group must choose

- a **moderator** to ensure the discussion focus on the **paper** : raise questions, identify main points, discuss possibilities and potentials
- a **reporter** to take notes (to be given to the team at end of session) and report back orally

10.00-10.25 Short reports from five groups + authors' final phrase (total  $\leq$  5 mins/paper)

NB: each **author** should take notes of points in the discussion and select one or two to mention at this point

10.25-10.30 Final remarks and comments on procedure



16:00 – 17:00 Welcome and paper reminder presentations + reactions

Liebendörfer, Sikko & Pepin, Stadler et al, Toor & Mgombelo, Bergster & Jablonka

17:00 – 17:30 Small group discussion per paper

17:30 – 18:00 Plenary short presentation and discussion

NB: each group must choose

– a **moderator** to ensure the discussion focus on the **paper** : raise questions, identify main points, discuss possibilities and potentials

– a **reporter** to take notes (to be given to the team at end of session) and report back orally

NB: each **author** should take notes of points in the discussion and select one or two to mention at this point

9:00 – 9:45 Welcome and paper reminder presentations + reactions

9:45 – 10:15 Small group discussion per paper

10:15 – 10:30 Plenary short presentation and discussion

NB: each group must choose

– a **moderator** to ensure the discussion focus on the **paper** : raise questions, identify main points, discuss possibilities and potentials

– a **reporter** to take notes (to be given to the team at end of session) and report back orally

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In CERME7 (2011)... 20 years after:

Tall, D. (1991). *Advanced Mathematical Thinking*.

Dordrecht: Kluwer Academic Publishers.

In CERME8 (2013)... 20 years after:

- Tall, D. (1992). The transition to Advanced Mathematical Thinking: Functions, Limits, Infinity, and Proof, in D. A. Grouws (ed.), *Handbook of Research on Mathematics Teaching and Learning* (pp. 495-514), New York: MacMillan Publishing Company.

11:00 – 11:45 Welcome and paper reminder presentations + reactions

11:45 – 12:15 Small group discussion per paper

12:15 – 12:30 Plenary short presentation and discussion

NB: each group must choose

– a **moderator** to ensure the discussion focus on the **paper** : raise questions, identify main points, discuss possibilities and potentials

– a **reporter** to take notes (to be given to the team at end of session) and report back orally

NB: each **author** should take notes of points in the discussion and select one or two to mention at this point

8:30 – 9:15 Welcome and paper reminder presentations + reactions

9:15 – 9:40 Small group discussion per paper

9:40– 10:00 Plenary short presentation and discussions preparation  
for session 7

NB: each group must choose

– a **moderator** to ensure the discussion focus on the **paper** : raise questions, identify main points, discuss possibilities and potentials

– a **reporter** to take notes (to be given to the team at end of session) and report back orally

NB: each **author** should take notes of points in the discussion and select one or two to mention at this point

**Discussion of posters, 10 mins**

**Preparing Sunday's WG14 presentation\*, 50 mins**

- Group work
- Plenary discussion

**Preparations for the Proceedings, 5 mins**

- WG14 leader team convenes and addresses invitations to authors to revise and submit their papers for consideration for inclusion in the proceedings by February 15
- Invited authors revise and resubmit **by April 1**
- Decisions about publication in the proceedings within April
- Possible outcomes: Accept, Short Contribution, Reject

**General discussion on WG structure, content and management, 10 mins**

**Post-conference collaboration, 15 mins**

- *RME Special Issue Proposal*
- *PME37?*
- *Beyond CERME8....*

## **Groups (4)**

- Transitions
- Affect
- teacher practices
- mathematical topics

## **Group work focus**

- Theory
- Research paradigms
- Results
- Rigour/quality

## **Group work output**

4 slides (max) to feed into the presentation

**Plenary discussion of group-work outputs and presentation drafting**



***Thank you!***  
***Stay in touch***  
***See you later...***

**WG14**

***University mathematics education***

**Sunday Presentation**

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- Mathematical reasoning and proof in university mathematics
- Challenges for teaching mathematics at university level (including the perspectives of university teachers)
- The role of ICT tools (e.g. CAS) in the teaching and learning of university mathematics
- Transition issues “at the entrance” to university studies of mathematics, or beyond
- Novel approaches to teaching Calculus and Linear Algebra
- The teaching and learning of advanced university mathematics topics (beyond Calculus and Linear Algebra)
- Challenges of teaching mathematics to students in non-mathematics degrees
- Assessing the learning and teaching of mathematics at university level
- Theoretical approaches to the study of teaching and learning mathematics at university

22 papers, organized in five themes:

*Transition (secondary/university)*

*Affects, students' interests*

*Teachers practices*

*Mathematical topics*

*Mathematical domains*

5 posters

## **Use of theory**

- Bergster & Jablonka: Bourdieu (cultural capital linked to other types of capital)
- Sikko & Pepin: transition literature
- Toor & Mgombelo: syncretic (compatible?)
- Liebendörfer: SDT (Krapp)
- Stadler et al: Stadler's own triad of concepts; advanced statistics

## Research paradigms

- Bergster & Jablonka : qualitative, pattern spotting
- Sikko & Pepin: quantitative / qualitative
- Toor & Mgombelo : concurrent mixed methods
- Liebendörfer: focus group interview, individual interview data, qualitative content analysis
- Stadler et al: bridging quantitative / qualitative paradigms

## **Results**

- Bergster & Jablonka : Culture and environment influence our choice of studies ways of coping with our studies
- Sikko & Pepin : Lectures do not attend to students' needs on how they learn best Peer work is a helpful survival technique.
- Toor & Mgombelo : gender differences in self image of capability
- Liebendörfer: demonstrate capacity of SDT tool
- Stadler et al: identify several differences between beginners and more experienced students



# Theoretical Frameworks

- Enculturation of mathematics / philosophy of mathematics (Hoffkamp, Schnieder & Paravicini)
- Task-design to support Transition (Breen, O'Shea & Pfeiffer)
- Student Errors (Fardinpour & Gooya)
- ATD (Winslow)
- Curriculum-(re-)design & Multiple representation (Schmidt)

# Paradigms

- Research-based development with evaluation / action research (Breen, O'Shea & Pfeiffer; Schmidt; Hoffkamp, Schnieder & Paravicini)
- Error analysis (Fardinpour & Gooya)
- Practice based development of theory (Winslow)

# Results

- Non-standard tasks can facilitate students' transition (Breen, O'Shea & Pfeiffer)
- Findings from Ireland confirm int. research results on students' problems (Breen, O'Shea & Pfeiffer)
- Beginning with complex numbers/functions can improve basic skills (Schmidt)
- Being explicit and intentional about metamathematical foundations can help students' thinking about mathematics (Hoffkamp, ...)
- Capstone courses assume an advanced standpoint in relevant mathematics (Winslow)
- Model captures difficulties students encounter with ODEs (Fardinpour & Gooya)

## Theory

– Used:

- Biza, Jaworski: Communities of practice and communities of enquiry
- Pinto: Planning curriculum and implemented curriculum
- Pinto: Decision making theory (Schoenfeld, 2011)
- Gueudet: Resources – Documentational genesis

– Further suggestions:

- Didactic situations
- Teacher knowledge at university level

- Research Paradigms
  - Biza: Analytical reflective practice: reflective practitioner analyses his/her practice (insider research)
  - Jaworski: Within socio-cultural frame, developmental study in which insider and outsider researchers work collaboratively.
  - Pinto, Gueudet: Ethnographic approach including observation and reflective analysis
  - Nardi: Literature study with implications for teaching
  - Gueudet, Pinto: Case study

- Results
  - Biza: Hypothesis generating for hypothesis testing
  - Gueudet: Importance of the articulation of paper/pencil and digital resources
  - Gueudet: Evolution of the collective work linked to the digital resources
  - Jaworski: Confirmation of the integrity of the design of teaching and of the problematic nature of discerning conceptual understanding leading to a theoretical reconceptualisation
  - Pinto: The impact of the teaching experience, agenda and identity on teachers' decision
  - Nardi: Proposition of teaching intervention for PGR students in mathematics education

## Theoretical approach

- « *Understanding* » (Berman, Hyvarinen, Pettersson, Schlarman)
- Theoretical diversity (commognition, ATD, cognitive approaches, ...).
- Older approaches (Skemp, Pierce).
- Richness.
- More cognitive approaches than in CERME7 (Alvarado, Berman, Hyvarinen, Pettersson, Schlarman).
- Using / cobining different frameworks (Alvarado, Berman, Pettersson) : use and misuse

- Research paradigms
  - More or less the same topics as in last CERME (functions, calculus, proof, linear algebra).
  - Sfard's framework is probably evolving to develop research methodologies (Viirman, Pettersson).
  - Methodologies we have used are really diverse.
  - Long-term studies (Alvarado, Hyvarinen, Pettersson).



- Results
  - A greater focus on teaching and predicting learning (Gonzalez-Martin, Viirman), epistemological approaches (Hausberger), constructive activities (Alvarado).
  - The focus is more on what you learn, how you learn it...
  - We would like to see more applications for teachers and want to share with teachers. Papers with mathematical notions are maybe easier to share.

### **Rigour / Quality**

- In practitioner research, subject and object of research can be too close
- Results are dependent on the context and on the local institution
- The collection of data relies only on practitioner's reflection
- Triangulation is needed
- Collection of data from different sources is needed
- Transparency of the nature of the interpretations
- Coherence - Is our framework adequate to address our problem ?
- Combination of frameworks and coherence and not incompatibility.
- Bias when the teacher is the researcher.
- Caution in the use of statistics
- nuance, ground for apparently self evident claims
- isolating slice of data for reporting
- need to further test
- emerging results, not ready yet for dissemination?
- small sample
- convenient sampling: opportunistic? Importance of context then!
- Hypotheses have to be verified in other contexts
- Strengthen theoretical models to improve validity of results